



Note: Objective part is compulsory. Attempt any four questions from subjective part.

Objective Part (Compulsory)

- Q.1. Write short answers of the following in 2-3 lines each. (16*2)
- Verify whether $(P \wedge Q) \rightarrow (P \vee Q)$ is tautology or not.
 - Let $Q(x)$ denote the statement " $x = x + 1$." What is the truth value of the quantification $\exists xQ(x)$, where the domain consists of all real numbers?
 - Suppose that the domain of the propositional function $P(x)$ consists of the integers 1, 2, 3, 4, and 5. Express these statements without using quantifiers $\neg \exists xP(x) \neg (P(1) \wedge P(2) \wedge P(3) \wedge P(4) \wedge P(5))$ Write in symbolic form "Some student have no ID cards".
 - Write the names of an algorithm properties?
 - What is the decimal expansion of the number with hexadecimal expansion (2AE0B)₁₆?
 - Define partial ordering with example.
 - Determine whether the integers 10, 17, and 21 are pairwise relatively prime?
 - Define the spanning tree of a graph.
 - Encrypt the message WATCH YOUR STEP by translating the letters into numbers, applying the given encryption function, and then translating the numbers back into letters. $f(p) = (14p + 21) \bmod 26$
 - How can you produce the terms of a sequence if the first 10 terms are 5, 11, 17, 23, 29, 35, 41, 47, 53, 59?
 - How many permutations of the letters ABCDEFG contain the string CFGA?
 - Find recurrence relation of the sequence $S(n) = 5^n$
 - How many subsets with more than two elements does a set with 100 elements have?
 - What are the connected components of a graph?
 - What is a bipartite graph?
 - What is the height of a rooted tree?

Subjective Part

- Q.2. Prove that if $m + n$ and $n + p$ are even integers, where m , n , and p are integers, then $m + p$ is even. What kind of proof did you use? [12]
- Q.3. Find each of these values. [12]
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|-------------------------------|-------------------------------|
| a) $(992 \bmod 32)3 \bmod 15$ | b) $(34 \bmod 17)2 \bmod 11$ |
| c) $(193 \bmod 23)2 \bmod 31$ | d) $(893 \bmod 79)4 \bmod 26$ |
- Q.4. Suppose that a password for a computer system must have at least 8, but no more than 12, characters, where each character in the password is a lowercase English letter, an uppercase English letter, a digit, or one of the six special characters *, >, <, !, +, and =. [6]
- How many different passwords are available for this computer system? [6]
 - How many of these passwords contain at least one occurrence of at least one of the six special characters? [12]
- Q.5. Find the smallest relation containing the relation $\{(1, 2), (1, 4), (3, 3), (4, 1)\}$ that is [12]
- Reflexive and transitive.
 - Symmetric and transitive.
 - Reflexive, symmetric, and transitive.
- Q.6. a) Using alphabetical order, construct a binary search tree for the words in the sentence "The quick brown fox jumps over the lazy dog." [12]
- b) Use Huffman coding to encode these symbols with given frequencies: a: 0.20, b: 0.10, c: 0.15, d: 0.25, e: 0.30. What is the average number of bits required to encode a character?
- Q.7. A coin is flipped 10 times where each flip comes up either heads or tails. How many possible outcomes [12]
- are there in total?
 - contain exactly two heads?
 - contain at most three tails?
 - contain the same number of heads and tails?